## CAT 2019 Question Paper Slot 2 I CAT Quants

Q1. The real root of the equation $26 x+23 x+2-21=0$ is
A. $\log 23 / 3$
B. $\log 29$
C. $\log 27 / 3$
D. $\log 227$

Q2: The average of 30 integers is 5 . Among these 30 integers, there are exactly 20 which do not exceed 5 . What is the highest possible value of the average of these 20 integers?
A. 4
B. 5
C. 4.5
D. 3.5

Q3: Let $a, b, x, y$ be real numbers such that $a 2+b 2=25, x 2+y 2=169$ and $a x+b y=65$. If $k=$ ay - bx, then
A. $k=0$
B. $k>5 / 13$
C. $k=5 / 13$
D. $0<k<=5 / 13$

Q4: In a triangle $A B C$, medians $A D$ and $B E$ are perpendicular to each other, and have lengths 12 cm and 9 cm , respectively. Then, the area of triangle $A B C$, in sq cm , is
A. 80
B. 68
C. 72
D. 78

Q5: Let a1, a2 be integers such that $\mathrm{a} 1-\mathrm{a} 2+\mathrm{a} 3-\mathrm{a} 4+\ldots \ldots . .+(-1) \mathrm{n}-1$ an $=\mathrm{n}$, for $\mathrm{n} \geq 1$. Then a51 $+\mathrm{a} 52+\ldots \ldots . .+\mathrm{a} 1023$ equals
A. -1
B. 1
C. 0
D. 10

Q6: How many factors of $24 \times 35 \times 104$ are perfect squares which are greater than 1 ? [TITA]
Q7: Two circles, each of radius 4 cm , touch externally. Each of these two circles is touched externally by a third circle. If these three circles have a common tangent, then the radius of the third circle, in cm , is
A. $\pi / 3$
B. 1
C. $1 / \sqrt{ } 2$
D. $\sqrt{ } 2$

Q8: What is the largest positive integer such that $n 2+7 n+12 / n 2-n-12$ is also positive integer?
A. 6
B. 8
C. 16
D. 12

Q9: In 2010, a library contained a total of 11500 books in two categories - fiction and non-fiction. In 2015, the library contained a total of 12760 books in these two categories. During this period, there was $10 \%$ increase in the fiction category while there was $12 \%$ increase in the non-fiction category. How many fiction books were in the library in $2015 ?$
A. 6600
B. 6160
C. 6000
D. 5500

Q10: Let $f$ be a function such that $f(m n)=f(m) f(n)$ for every positive integers $m$ and $n$. If $f(1), f$ (2) and $f(3)$ are positive integers, $f(1)<f(2)$, and $f(24)=54$, then $f(18)$ equals [TITA]

Q11: Let $A$ and $B$ be two regular polygons having $a$ and $b$ sides, respectively. If $b=2 a$ and each interior angle of $B$ is $3 / 2$ times each interior angle of $A$, then each interior angle, in degrees, of a regular polygon with $a+b$ sides is [TITA]

Q12: A cyclist leaves $A$ at 10 am and reaches $B$ at 11 am . Starting from 10:01 am, every minute a motorcycle leaves $A$ and moves towards B. Forty-five such motorcycles reach B by 11 am . All motorcycles have the same speed. If the cyclist had doubled his speed, how many motorcycles would have reached $B$ by the time the cyclist reached $B$ ?
A. 22
B. 20
C. 15
D. 23

Q13: Let $A$ be a real number. Then the roots of the equation $x 2-4 x-\log 2 A=0$ are real and distinct if and only if
A. $A<1 / 16$
B. $A>1 / 8$
C. $A>1 / 16$
D. $A<1 / 8$

Q14: John jogs on track $A$ at 6 kmph and Mary jogs on track $B$ at 7.5 kmph . The total length of tracks $A$ and $B$ is 325 metres. While John makes 9 rounds of trackA, Mary makes 5 rounds of track B. In how many seconds will Mary make one round of track A? [TITA]

Q15: Anil alone can do a job in 20 days while Sunil alone can do it in 40 days. Anil starts the job, and after 3 days, Sunil joins him. Again, after a few more days, Bimal joins them and they together finish the job. If Bimal has done $10 \%$ of the job, then in how many days was the job done?
A. 13
B. 12
C. 15
D. 14

Q16: In an examination, Rama's score was one-twelfth of the sum of the scores of Mohan and Anjali. After a review, the score of each of them increased by 6. The revised scores of Anjali, Mohan, and Rama were in the ratio 11:10:3. Then Anjali's score exceeded Rama's score by
A. 26
B. 32
C. 24
D. 35

Q17: In an examination, the score of $A$ was $10 \%$ less than that of $B$, the score of $B$ was $25 \%$ more than that of $C$, and the score of $C$ was $20 \%$ less than that of $D$. If $A$ scored 72 , then the score of D was [TITA]

Q18: The base of a regular pyramid is a square and each of the other four sides is an equilateral triangle, length of each side being 20 cm . The vertical height of the pyramid, in cm , is
A. $10 \sqrt{ } 2$
B. $8 \sqrt{ } 3$
C. 12
D. $5 \sqrt{ } 5$

Q19: If $x$ is a real number, then $\sqrt{ }$ loge $(4 x-x 2)$ is a real number if and only if
A. $-3 \leq x \leq 3$
B. $1 \leq x \leq 2$
C. $1 \leq x \leq 3$
D. $-1 \leq x \leq 3$

Q20: Let $A B C$ be a right-angled triangle with hypotenuse $B C$ of length 20 cm . If $A P$ is perpendicular on $B C$, then the maximum possible length of $A P$, in cm , is
A. 10
B. $8 \sqrt{ } 2$
C. $6 \sqrt{ } 3$
D. 5

Q21: Two ants $A$ and $B$ start from a point $P$ on a circle at the same time, with $A$ moving clock-wise and $B$ moving anti-clockwise. They meet for the first time at 10:00 am when $A$ has covered $60 \%$ of the track. If $A$ returns to $P$ at 10:12 am, then $B$ returns to $P$ at
A. 10:27 am
B. $10: 25 \mathrm{am}$
C. $10: 45 \mathrm{am}$
D. $10: 18 \mathrm{am}$

Q22: How many pairs $(m, n)$ of positive integers satisfy the equation the equation $m 2+105=$ n2? [TITA]

Q23: The salaries of Ramesh, Ganesh and Rajesh were in the ratio 6:5:7 in 2010, and in the ratio $3: 4: 3$ in 2015 . If Ramesh's salary increased by $25 \%$ during 2010-2015, then the percentage increase in Rajesh's salary during this period is closest to
A. 7
B. 8
C. 9
D. 10

Q24: A man makes complete use of 405 cc of iron, 783 cc of aluminium, and 351 cc of copper to make a number of solid right circular cylinders of each type of metal. These cylinders have the same volume and each of these has radius 3 cm . If the total number of cylinders is to be kept at a minimum, then the total surface area of all these cylinders, in sq cm , is
A. $1044(4+\pi)$
B. $8464 \pi$
C. $928 \pi$
D. $1026(1+\pi)$

Q25: The quadratic equation $\mathrm{x} 2+\mathrm{bx}+\mathrm{c}=0$ has two roots 4 a and 3 a , where a is an integer. Which of the following is a possible value of $b 2+c$ ?
A. 3721
B. 549
C. 361
D. 427

Q26: In a six-digit number, the sixth, that is, the rightmost, digit is the sum of the first three digits, the fifth digit is the sum of first two digits, the third digit is equal to the first digit, the second digit is twice the first digit and the fourth digit is the sum of fifth and sixth digits. Then, the largest possible value of the fourth digit is [TITA]

Q27: Mukesh purchased 10 bicycles in 2017, all at the same price. He sold six of these at a profit of $25 \%$ and the remaining four at a loss of $25 \%$. If he made a total profit of Rs. 2000 , then his purchase price of a bicycle, in Rupees, was
A. 2000
B. 6000
C. 8000
D. 4000

Q28: The number of common terms in the two sequences: $15,19,23,27, \ldots \ldots, 415$ and 14,19 , $24,29, \ldots \ldots ., 464$ is
A. 20
B. 18
C. 21
D. 19

Q29: If $(2 n+1)+(2 n+3)+(2 n+5)+\ldots+(2 n+47)=5280$, then what is the value of $1+2+3+\ldots+n$ ? [TITA]

Q30: The strength of a salt solution is $\mathrm{p} \%$ if 100 ml of the solution contains p grams of salt. Each of three vessels A, B, C contains 500 ml of salt solution of strengths $10 \%, 22 \%$, and $32 \%$, respectively. Now, 100 ml of the solution in vessel $A$ is transferred to vessel $B$. Then, 100 ml of the solution in vessel $B$ is transferred to vessel C. Finally, 100 ml of the solution in vessel $C$ is transferred to vesselA. The strength, in percentage, of the resulting solution in vessel $A$ is
A. 15
B. 12
C. 13
D. 14

Q31: If $5 x-3 y=13438$ and $5 x-1+3 y+1=9686$, then $x+y$ equals [TITA]
Q32: Amal invests Rs 12000 at 8\% interest, compounded annually, and Rs 10000 at 6\% interest, compounded semi-annually, both investments being for one year. Bimal invests his money at $7.5 \%$ simple interest for one year. If Amal and Bimal get the same amount of interest, then the amount, in Rupees, invested by Bimal is [TITA]

Q33: A shopkeeper sells two tables, each procured at cost price p, to Amal and Asim at a profit of $20 \%$ and at a loss of $20 \%$, respectively. Amal sells his table to Bimal at a profit of $30 \%$, while Asim sells his table to Barun at a loss of $30 \%$. If the amounts paid by Bimal and Barun are x and $y$, respectively, then $(x-y) / p$ equals
A. 1
B. 1.2
C. 0.7
D. 0.50

Q34: John gets Rs 57 per hour of regular work and Rs 114 per hour of overtime work. He works altogether 172 hours and his income from overtime hours is $15 \%$ of his income from regular hours. Then, for how many hours did he work overtime? [TITA]

