$-\ell)^2 \leq NS \leq \pi (R+\ell)^2$ ρ +2 Goliveboard = ns F.  $= q + M \hat{P} \hat{O} \hat{P} \hat$ MATHSSHORT FORMULAS n<sub>2</sub> (φ, p)  $\theta + isin \theta$  =  $\sqrt[3]{\Gamma} \left( \cos \frac{\theta}{5} + i \sin \frac{\theta}{3} \right)$ = Pn (cosd) =Qn (cosd). sind fo (x,y) = 1 x2+ y2 ccudu 1 2 (1xy1+14

For Bank, SSC, Railway and Insurance Exams

### **NUMBER SYSTEM**

### Method to multiply 2-digit number.

AB × CD = AC {AD + BC} BD 63\*46 = 24 {36 + 12} 18 Add the middle term = 24 {48} 18 Keep first term intact, form the middle term by adding 2 numbers also keep the last term same, which means 2 (4+4) (8+1) 8 = 2898

## Divisibility

Numbers	IF A Number	
Divisible by 2	End with 0,2,4,6,8 are divisible	
	by 2	
Divisible by 3	Sum of its digits is divisible by 3	
Divisible by 4	Last two digit divisible by 4	
Divisible by 5	Ends with 0 or 5	
Divisible by 6	Divides by Both 2 & 3	
Divisible by 8	Last 3 digit divide by 8	
Divisible by 10	End with 0	
Divisible by 11	[Sum of its digit in odd places-	
	Sum of its digits in even places]	
	= 0 or multiple of 11	
Divisible by 12	[The number must be divisible	
	by 3 and 4]	
Divisible by 13	[Multiply last digit with 4 and	
	add it to remaining number in	
	given number, result must be	
	divisible by 13]	
Divisible by 14	[The number must be divisible	
	by 2 and 7. Because 2 and 7 are	
	prime factors of 14.]	
Divisible by 15	[The number should be divisible	
	by 3 and 5. Because 3 and 5 are	
	prime factors of 15.]	

Goliveboard

Divisible by 16	[The number formed by last	
	four digits in given number	
	must be divisible by 16.]	
Divisible by 17	[Multiply last digit with 5 and	
	subtract it from remaining	
	number in given number, result	
	must be divisible by 17]	
Divisible by 18	[The number should be divisible	
	by 2 and 9]	
Divisible by 19	[Multiply last digit with 2 and	
	add it to remaining number in	
	given number, result must be	
	divisible by 19]	
Divisible by 20	[The number formed by last	
	two digits in given number must	

### **Division & Remainder Rules**

A very basic formula for division rules is:

dividend = (divisor **X** quotient) + remainder

or

divisor= [(dividend)-(remainder] / quotient

This could be mathematically written in another way:

 $\Rightarrow$  x = kq + r where (x = dividend, k = divisor, q = quotient, r = remainder).



### Sum Rules:

- Sum of first n natural numbers= n(n+1)/2
- Sum of square of first n natural numbers= n(n+1)(2n+1)/6
- Sum of cubes of first n natural numbers= (n(n+1)/2)^2
- Sum of first n odd numbers= n^2
- Sum of first n even numbers= n(n+1)

### Number of divisors:

- (i) If N is any no. and N = an  $\times$  bm  $\times$  cp  $\times$  .... where a, b, c is prime no.
- (ii) No. of divisors of N = (n + 1) (m + 1) (p + 1) ...

### ALGEBRA:

(i) 
$$(a + b)^2 + (a - b)^2 = 2 (a^2 + b^2)$$

- (ii)  $(a + b)^2 (a b)^2 = 4ab$
- (iii) $a^3 + b^3 = (a + b) (a^2 ab + b^2)$
- (iv)  $a^3 b^3 = (a b) (a^2 + ab + b^2)$
- (v)  $a^4 + a^2 + 1 = (a^2 + a + 1) (a^2 a + 1)$
- (vi) If a + b + c = 0, then  $a^3 + b^3 + c^3 = 3abc$

(vii) 
$$\frac{(a+b)^2 - (a-b)^2}{ab} = 4$$
  
(viii) 
$$\frac{(a+b)^2 + (a-b)^2}{a^2 + b^2} = 2$$

- (ix) If  $a_1x + b_1y = c_1$  and  $a_2x + b_2y = c_2$ , then
  - (a)  $a_1/a_2 \neq b_1/b_2$ , one solution
  - (b)  $a_1/a_2 = b_1/b_2 = c_1/c_2$ , infinitely many solution
  - (c)  $a_1/a_2 = b_1/b_2 \neq c_1/c_2$ , No Solution

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### **Arithmetic Progression:**

If a, a + d, a + 2d, .... are in A.P., then, nth term of A.P. an = a + (n - 1) d Sum of n terms of this A.P = Sn = n/2 [2a + (n-1) d] Where: a = first term d = common difference

### **Geometric Progression:**

(i) G.P. = a, ar,  $ar^2$ , ..... Then, nth term of G.P.  $a_n = ar^{n-1}$ 

Sum of n numbers Sn = a  $(r^{n}-1)/r-1$ , For r>1

= a (1 - r<sup>n</sup>)/ 1-r, for r<1

### **AVERAGE:**

- (i) Average of first n natural no. = (n=1)/2
- (ii) Average of first n even no. = (n + 1)
- (iii) Average of first n odd no. = n
- (iv) Average of sum of square of first n natural no. = (n+1)(2n+1)/6
- (v) Average of sum of square of first n even no. = 2(n+1)(2n+1)/3
- (vi) Average of sum of square of first odd no = (4n2 1)/3
- (vii) If average of some observations is x and a is added in each observation, then new average is (x + a).
- (viii) If average of some observations is x and a is subtracted in each observation, then new average is (x a).
- (ix) If average of some observations is x and each observation multiply by a, then new average is ax.
- If average of some observations is x and each observation is divided by a, then new average is x/a



## **RATIO & PROPORTION:**

- (i)  $A/k1 = b/K2 = c/K3 \dots$  then  $(a+b+c+\dots)/c = (K1+K2+K3+\dots)/K3$
- (ii) A number added or subtracted from a, b, c & d, so that they are in proportion =  $\frac{ad-bc}{(a+d)-(b+c)}$

## TIME & WORK:

(i) A can-do a/b part of work in t1 days and c/d part of work in t2 days,  $t_1$   $t_2$ 

then  $\frac{t_1}{a_{/b}} = \frac{t_2}{c/d}$ 

(a) If A is K times efficient than B, Then  $T(K + 1) = Kt_B$ 

(b) If A is K times efficient than B and takes t days less than B, then T = t/(k-1)& tb = t/k-1 = Kt<sub>A</sub>

 (iii) If a cistern takes X min to be filled by a pipe but due to a leak, it takes Y extra minutes to be filled, then the time taken by leak to empty the cistern

$$= (X^2 + XY)/Y \min$$

- (iv) If a leak empties a cistern in X hours. A pipe which admits Y litres per hour water into the cistern and now cistern is emptied in Z hours, then capacity of cistern is = (X+Y+Z)/(Z-X)
- (v) If t1 and t2 time taken to travel from A to B and B to A, with speed a km/h and b km/h, then distance from A to B is

$$d = (t_1 + t_2) \left(\frac{ab}{a+b}\right)$$
 or  $d = (t_1 - t_2) \left(\frac{ab}{a-b}\right)$ 

$$d = (a-b)\left(\frac{t_1t_2}{t_1-t_2}\right)$$





### **PERCENTAGE:**

Simple Fraction	Percentage
1	100%
1/2	50%
1/3	33.3%
1/4	25%
1/5	20%
1/6	16.67%
1/7	14.28%
1/8	12.50%
1/9	11.11%
1/10	10.00%
1/11	9.09%
1/12	8.33%

- (i) If A is (x% = a/b) more than B, then B is  $\frac{a}{a+b}$ % less than A.
- (ii) If A is (x% = a/b) more than B, then B is  $\frac{a}{a-b}\%$  more than A. if a > b, we take a - bif b > a, we take b - a.
- (iii) If price of a article increase from Rs 'a' to Rs 'b', then its expenses decrease by  $\left(\frac{b-a}{\dot{b}} \times 100\right)$ % that expenditure will be same.
- (iv) Due to increase/decrease the price x%, A man purchase a kg more in `y, then Per kg increase or decrease = (XY/100\*a)



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### For 2 Articles, If price:

lst	lInd	Overall
Increase	Increase	Increase
(x%)	(y%)	$\left(x + y + \frac{xy}{100}\right)\%$
Increase (x%)	Decrease (y%)	$\left(x - y - \frac{xy}{100}\right)$ % if +ve (increase) if -ve (decrease)
Decrease	Decrease	Decrease
(x%)	(y%)	$\left(x + y - \frac{xy}{100}\right)\%$
Increase	Decrease	Decrease
(x%)	(x%)	(X²/100) %

- (v) If the side of a square or radius of a circle is x% increase/decrease, then its area increase/decrease = (2X ± X<sup>2</sup>/100) %
- (vi) If the side of a square, x% increase/decrease then x% its perimeter and diagonal increase/decrease.
- (vii) If population P increase/decrease at r% rate, then after t years population  $P\left\{\frac{100\pm R}{100}\right\}^{t}$
- (viii) If a man spends **x%** of this income on food, **y%** of remaining on rent and **z%** of remaining on cloths. If he has `P remaining, then total income of man is =  $\frac{P \times 100^3}{(100-x)(100-y)(100-2)}$



### SIMPLE & COMPOUND INTEREST:

If P = Principal, R = Rate per annum, T = Time in years, SI = Simple interest, A = Amount

- (i) Simple Interest = PRT/100
- (ii) Amount = Principle + Simple Interest = P[1+RT/100]
- (iii) If P = Principal, A = Amount in n years, R = rate of interest per annum. Then
  A= P [1+ R/100]<sup>n</sup>, interest payable annually. For Half-yearly interest R = r/2
  - For Quarterly interest R = r/4
- (iv)  $CI = Amount Principal = P[(1+R/100)^{n} 1]$
- (v) When Rates are different for different years, say R1, R2, R3% for 1st, 2nd & 3rd years respectively, then, Amount = P[1+R<sub>1</sub>/100] [1+R<sub>2</sub>/100] [1+R<sub>3</sub>/100]

### Few Tricks for Faster Math Calculations:

 Finding square of numbers having 5 unit digit- Suppose a number 55 is given to you, all you need to do is square the 5 at units place and multiply the number at 10's place with its succeeding number, in this case 6.

So it makes (55)<sup>2</sup> = (5\*6)25 = **3025** Example: (75)2 = (7\*8)25 = **5625** 

**2.** Multiplying a number by 11- If you must multiply a number by 11, here are few very basic steps that will reduce your calculations to your fingers.

Example: 23\*11 = Take the number 23, put 2&3 at 100's and unit place, 2()3. In the blank in between put the total of units and 100s place, which makes it 2(2+3)3 = 253 which is the answer.

There is one exception to this condition, when the total of mid term exceeds 10, add the 1 from 10 in the first digit.



### Example: 59\*11 = 5(5+9)9 = 5(14)9 = (5+1)49 = 649

**3.** Division by 5: If a number is given to be divided by 5, all you need to do is just double the given number and move the decimal point to 1 place left.

Example – 350/5, multiply 350 by 2 which makes it 700, now move the decimal to 1 place left. Therefore, answer **is 70** 

**4. Multiplying a number by 5:** To multiply a number by, it may seem easy for smaller number but when it comes to 3- or 4-digit number you might feel the pain. Don't worry here is a super trick to approach. If you must multiply a number by 5, just divide the given number by 2 and add 0 at the end, in case of decimal move it one step right.

**Example:** 124\*5. Divide 124 by 2, which makes it 62, now add a zero at the end, which makes **it 620**, and that is your answer.

5. Multiplying a number by 9: Suppose you wish to multiply a number by 9. Let take an example, 72\*9. All you need to do is add 0 at the end of number other than 9 here it is 72, which makes it 720. Now subtract the original number from 720. The answer becomes 648.

These are few faster solving techniques and formulas that will help you increase your confidence and efficiency and will reduce your time consumptions.





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